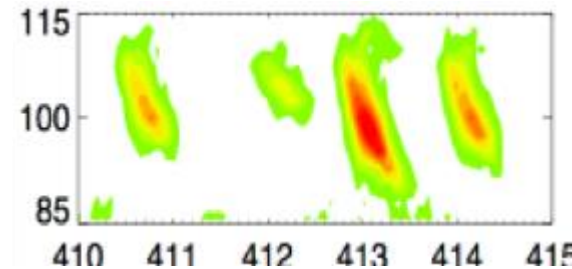
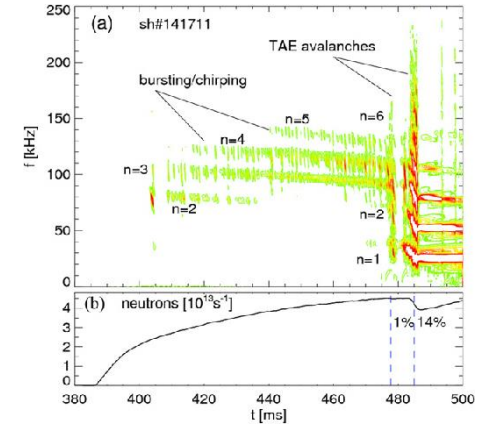




- Significant excitation of toroidicity-induced Alfvén eigenmodes (TAEs) were observed in NSTX 141711 with NBI (Podesta NF 2012)
 - Down-chirping and chirping of TAE with $n=1-6$ characterized by period of $<1\text{ms}$.
 - TAE avalanche can be triggered by large down-chirping, resulting in significant EP loss.

TAE spectrum in NSTX #141711

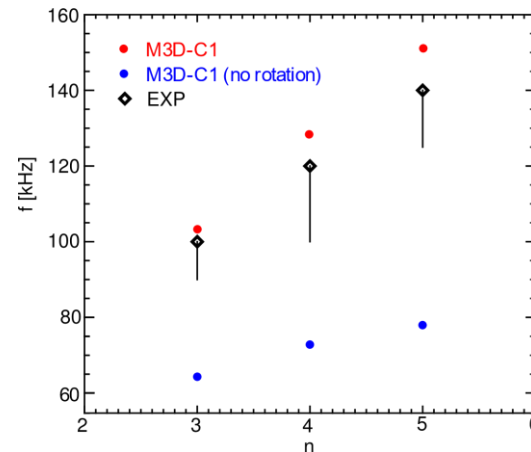
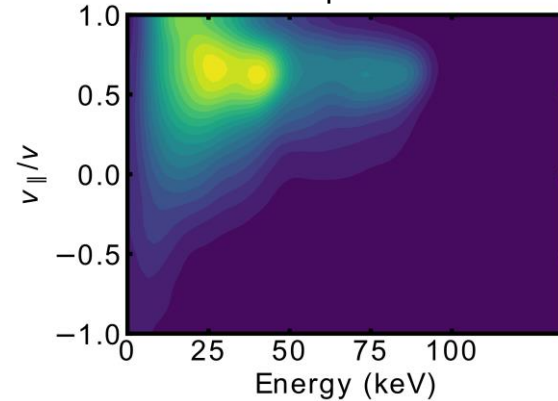


Frequency and amplitude evolution during TAE chirping



- Kinetic-MHD code M3D-C1-K was upgraded to simulate Alfvén eigenmodes in NSTX driven by high-energy beam particles.
 - Classical EP distribution calculated using NUBEAM was used for particles initialization and δf calculation.
 - Toroidal rotation profile can be included in both MHD and particle simulation.
- TAE frequencies from linear simulation are consistent with experiments and previous M3D-K results (D. Liu PoP 2015)
 - Frequency spacing between different n modes comes from both dispersion of TAE and Doppler shift of rotation.

EP distribution at core read from NUBEAM output

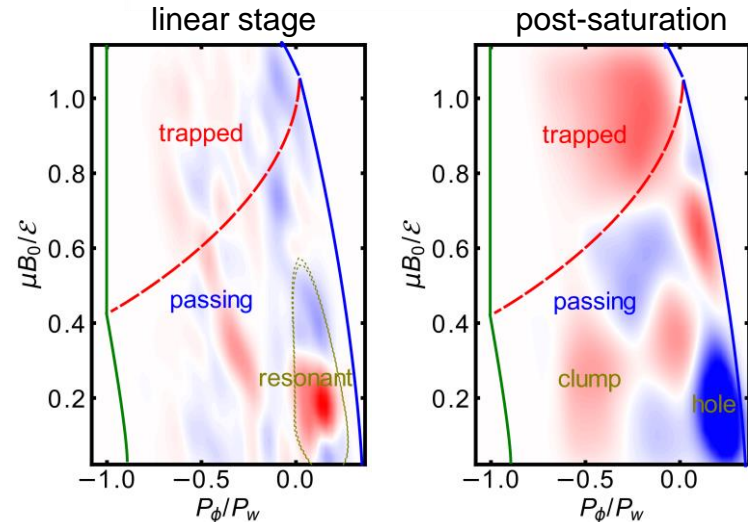
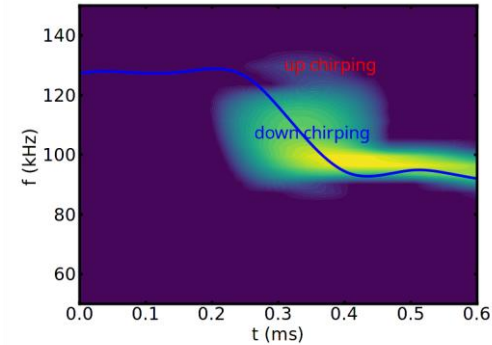


TAE frequencies from linear simulation compared with experiments



- By enabling the nonlinear terms in the kinetic simulation, the frequency chirping of the mode can be reproduced.
 - Down-chirping dominates, which is consistent with experiments
 - Chirping timescale consistent with experiment (<1ms)
- Analysis of particle phase space reveals the dominant wave-particle resonance comes from passing particles near resonant flux surface.
- In the saturation stage, resonant particles get splitted into clump and hole regions moving in different directions, consistent with the frequency chirping theory.

TAE spectrogram from nonlinear M3D-C1 simulation





irotp=1 eqsubtract=1

- Numerical instability can arise when using ifbound=1
 - Setting ifbound=2 seems help. Maybe due to this damping term:

```
if(ifbound.eq.2) then
    r_bf = r_bf - regular*intx3(trial(:, :, OP_1), r2_79, lin(:, OP_1))
end if
```

- May also be related to non-zero edge rotation
- Using semi-implicit method with thimp=1.0 can lead to suppression of TAE when rotation velocity is large
 - Can be avoided by forcing Crank-Nicholson for convection due to v_0

```
tempx = v2vun(trialx, vz079, lin, rho79)
ssterm(:, u_g) = ssterm(:, u_g) - 0.5 * dt * tempx
ddterm(:, u_g) = ddterm(:, u_g) + (1.-0.5*bdf)*dt*tempx
```

- Using Caramana method (imp_mod=1) can lead to numerical instability when irot=1